

Reg No.: \_\_\_\_\_

Name: \_\_\_\_\_

**APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY**  
SIXTH SEMESTER B.TECH DEGREE EXAMINATION, APRIL 2018

**Course Code: EE304**

**Course Name: ADVANCED CONTROL THEORY (EE)**

Max. Marks: 100

Duration: 3 Hours

**PART A**

*Answer all questions, each carries 5 marks.*

Marks

- 1 What is a lag compensator? Draw its pole-zero plot and the frequency response characteristics. (5)
- 2 Explain the effects of adding PID controller to a system. (5)
- 3 Selecting  $i_1(t) = x_1(t)$  and  $i_2(t) = x_2(t)$  as state variables obtain state equation and output equation of the network shown in Fig.1 (5)

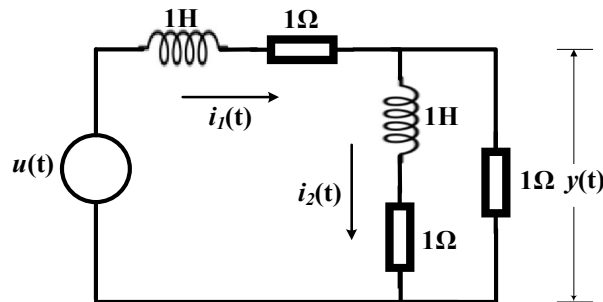


Fig.1

- 4 The characteristic polynomial of certain sampled data system is given by  $P(z) = z^4 - 1.2z^3 + 0.07z^2 + 0.3z - 0.08 = 0$ , test the stability of the system using Jury's stability test. (5)
- 5 Explain different non linearities with diagram. (5)
- 6 What is limit cycle? How will you determine stable and unstable limit cycle using phase portrait? (5)
- 7 What are singular point? Explain the types of singular point. (5)
- 8 Determine given quadratic form is positive definite or not (5)  
 $V(x) = 10x_1^2 + 4x_2^2 + x_3^2 + 2x_1x_2 - 2x_2x_3 - 4x_1x_3$

**PART B**

*Answer any two full questions, each carries 10 marks.*

- 9 a) For a feedback system shown in Fig. 2, design suitable compensator so that phase margin is  $40^\circ$  and steady state error for ramp input  $\leq 0.2$  (10)

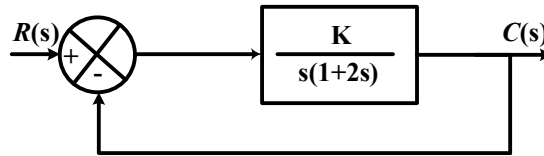


Fig. 2

- 10 Design a suitable compensator for the system with open-loop transfer function (10)  

$$G(s)H(s) = \frac{1}{s(s+1)(s+2)}$$
 so that the over shoot to a unit step input to be limited to 20% and the transient to be settled with in 3s.
- 11 a) Briefly explain Ziegler – Nichol’s PID tuning rules. (6)  
 b) Write the design steps of lead compensator based on frequency domain approach. (4)

### PART C

*Answer any two full questions, each carries 10 marks.*

- 12 Find the complete response of the system (10)

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} x + \begin{bmatrix} 2 & 1 \\ 0 & 1 \end{bmatrix} U(t), x(0) = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

and  $y(t) = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix} x$  to the following input,  $U(t) = \begin{bmatrix} u(t) \\ e^{3t}u(t) \end{bmatrix}$  where  $u(t)$  is the unit step input.

- 13 a) Transform the system in to controllable canonical form (7)

$$\dot{x} = \begin{bmatrix} -1 & 1 \\ 0 & 2 \end{bmatrix} x + \begin{bmatrix} 2 \\ 1 \end{bmatrix} u \text{ and } y = [1 \quad 2]x$$

- b) State and explain sampling theorem (3)

- 14 a) Consider a system defined by (7)

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ -3 & 1 \end{bmatrix} x + \begin{bmatrix} 0 \\ 2 \end{bmatrix} u \text{ and } y = [1 \quad 0]x$$

Using state feedback control  $u = -Kx$ , it is desired to have the closed loop poles at  $s = -3$  and  $s = -4$ , determine the state feedback gain matrix  $K$ .

- b) What is pulse transfer function? (3)

### PART D

*Answer any two full questions, each carries 10 marks.*

- 15 Obtain the describing function of saturation non-linearity (10)

- 16 A common form of an electronic oscillator is represented as shown in Fig. 3. For (10)  
 what value of  $K$ , the possibility of limit cycle predicted? If  $K=3$ , determine amplitude and frequency of limit cycle. Also find the maximum value of  $K$  for the

system is stable.

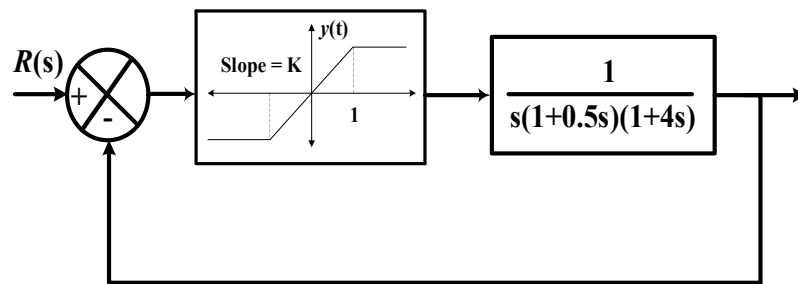


Fig. 3

17

A second order system is represented by  $\dot{x} = Ax$  where

(10)

$$A = \begin{bmatrix} 0 & 1 \\ -1 & -1 \end{bmatrix}$$

Assuming matrix  $Q$  to be identity matrix, solve for matrix  $P$  in the equation  $A^T P + P A = -Q$ . Use Lyapunov theorem and determine the stability of the system. Write the Lyapunov function  $V(x)$

\*\*\*\*