

Reg No.: _____

Name: _____

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY
Third Semester B.Tech (minor) Degree Examination December 2020

Course Code: ECT285

Course Name: INTRODUCTION TO SIGNALS AND SYSTEMS

Max. Marks: 100

Duration: 3 Hours

PART A

Answer all questions. Each question carries 3 marks

Marks

- | | | |
|----|--|-----|
| 1 | Distinguish between deterministic and random signals with suitable example. | (3) |
| 2 | Find the energy of the continuous signal $x(t) = e^{-2t} u(t)$. | (3) |
| 3 | Differentiate between discrete time periodic and non-periodic signals with example. | (3) |
| 4 | Define the signal $u(n)$ and hence sketch the sequence $u(n+2)-2u(n)+u(n-2)$. | (3) |
| 5 | Define Linearity and Shift invariance property in systems. | (3) |
| 6 | What is BIBO stability? | (3) |
| 7 | Find the autocorrelation of the sequence $x(n) = \{3,2,4,1\}$ for n in range $0:3$. | (3) |
| 8 | What are the properties of convolution sum? | (3) |
| 9 | Explain sampling theorem. | (3) |
| 10 | Comment about the spectrum of Continuous Time and Discrete Time Fourier transformed signals. | (3) |

PART B

Answer any one full question from each module. Each question carries 14 marks

Module 1

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|----|--|-----|
| 11 | (a) Define and sketch the following continuous time signals: | (6) |
| | (i) unit impulse function (ii) unit step function | |
| | (b) Find the even and odd components of the given signals: | (8) |
| | (i) $x(t) = e^{j2t}$ (ii) $x(t) = [\sin(\pi t) + \cos(\pi t)]^2$ | |
| 12 | (a) For a given composite signal $x(t)$ which is the sum of two periodic signals, explain the steps involved to determine its periodicity condition. | (6) |
| | (b) Sketch the following signal $x(t) = u(t+2) - u(t-2)$. Also determine whether the given signal is a power signal or energy signal or neither. | (8) |

Module 2

- 13 (a) If $x(n] = (1,2,-1,0,2,1,1,0,-1)$; $-4 \leq n \leq 4$, plot the following sequences (6)
- (i) $x(n-3)$ (ii) $x(-n)$
- (b) Determine whether the sequence $x(n] = \sin\left(\frac{6\pi n}{7}\right) + \sin\left(\frac{\pi n}{8}\right)$ is periodic or not. If periodic, determine the fundamental period. (8)
- 14 (a) A discrete time sequence is given by $x(n] = (1,1,1,1,2,2)$. Sketch (8)
- (i) $x(n] - x(n-2)$
- (ii) $x(n]u(n+2)$
- (b) Describe any two standard discrete time signals. (6)

Module 3

- 15 (a) Determine whether the following systems are Linear or Non Linear. (8)
- (i) $y(t] = x^2(t)$
- (ii) $y(n] = e^{x(n)}$
- (b) Explain stability and causality of a system. (6)
- 16 (a) Explain Static and Dynamic Systems. Is the discrete time system described by the equation $y(n] = x(n-1)$ is static or dynamic? (6)
- (b) Determine whether the following systems are Shift invariant or not. (8)
- (i) $y(t] = x(-t)$
- (ii) $y(n] = A x(n] + B$

Module 4

- 17 (a) Consider a discrete time LTI system with impulse response $h(n]$ given by $h(n] = (1/2)^n u(n)$. Determine if the system is Causal and BIBO stable? (8)
- (b) Find the output signal $y(n]$ of an LTI system ,if the input sequence is $x(n] = \{1,1,1,1\}$ and impulse response $h(n] = \{2,2\}$. (6)
- 18 (a) Find the convolution of the signal, (8)
- $$\begin{aligned} x(t] &= e^{-t} && ; t \geq 0 \\ &= 0 && ; t < 0 \end{aligned} \quad \text{with the signal}$$
- $$\begin{aligned} h(t] &= 1 && ; 0 \leq t \leq 3 \\ &= 0 && ; \text{otherwise} \end{aligned}$$

- (b) Prove that convolution of a function $x(t)$ with a unit impulse function $\delta(t)$ results in the function $x(t)$ itself. (6)

Module 5

- 19 (a) An analog signal is expressed by the equation

$$x(t) = \frac{1}{\pi} [\cos(5000\pi t) + \cos(3000\pi t)] \quad (6)$$

Calculate the Nyquist rate ?

- (b) Find the DTFT of sequences.

- (i) Unit impulse (8)

(ii) $x(n) = \left(\frac{1}{2}\right)^n u(n)$

- 20 (a) State and prove Parseval's theorem for discrete time Fourier transform. (6)

- (b) Find the CTFT of the signals.

- (i) $x(t) = \cos(\omega_0 t)$ (8)

- (ii) $x(t) = 1 ; -T \leq t \leq T$
 $= 0; \text{ otherwise}$
